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Reg No.: Name:

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

SECOND SEMESTER B.TECH DEGREE EXAMINATION, DECEMBER 2018

Course Code: MA102

Course Name: DIFFERENTIAL EQUATIONS

Max. Marks: 100 Duration: 3 Hours

PART A

Answer all questions, each carries 3 marks

1	Find a general solution of the ordinary differential equation $y'' + y = 0$	(3)
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- 2 Find the Wronskian of $e^x \cos 2x$ and $e^x \sin 2x$ (3)
- Find the particular integral of the differential equation y'' + y = cosh5x (3)
- 4 Using a suitable transformation, convert the differential equation.

$$(3x+2)^2y'' + 5(3x+2)y' - 3y = x^2 + x + 1$$
 into a linear differential (3) equation with constant coefficients.

- If f(x) is a periodic function of period 2L defined in [-L, L]. Write down Euler's Formulas a_0 , a_n , b_n for f(x).
- 6 Find the Fourier cosine series of $f(x) = x^2$ in $0 < x \le c$. (3)

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- Find the partial differential equation of all spheres of fixed radius having their centres in xy-plane. (3)
- Find the particular integral of $r + s 2t = \sqrt{2x + y}$. (3)
- Write any three assumptions involved in the derivation of one dimensional wave equation. (3)
- Solve $x \frac{\partial u}{\partial x} 2y \frac{\partial u}{\partial y} = 0$ using method of separation of variables. (3)
- Find the steady state temperature distribution in a rod of 30 cm having its ends at 20°C and 80°C respectively.
- Write down the possible solutions of the one dimensional heat equation. (3)

PART B

Answer six questions, one full question from each module

Module 1

- 13 a) Solve the initial value problem y'' + 4y' + 5y = 0, y(0) = 2, y'(0) = -5. (5)
 - b) Find a basis of solutions of the ODE $(x^2 x)y'' xy' + y = 0$, if $y_1 = x$ is a (6)

A S2035 Pages: 3

solution.

OR

14 a) Reduce to first order and solve
$$y'' + (1 + \frac{1}{y})(y')^2 = 0$$
 (5)

b) Solve the initial value problem 9y'' - 30y' + 25y = 0, y(0) = 3, y'(0) = 10. (6)

Module 1I

15 a) Solve
$$y'' - 2y' + 5y = e^{2x} \sin x$$
. (5)

b) Using method variation of parameters solve y'' + 4y = tan2x (6)

OR

16 a) Solve
$$x^3y''' + 3x^2y'' + xy' + y = x + \log x$$
 (5)

b) Solve using method of variation of parameters $y'' - 2y' + y = \frac{e^x}{x}$ (6)

Module 1II

Find the Fourier series of periodic function $f(x) = \begin{cases} -x, -1 \le x \le 0 \\ x, 0 \le x \le 1 \end{cases}$ with period 2. Hence prove that $1 + \frac{1}{3^2} + \frac{1}{5^2} + \cdots = \frac{\pi^2}{8}$.

OF

Find the Fourier series of periodic function $f(x) = x \sin x$, $0 < x < 2\pi$ with period 2π .

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Module 1V

19 a) Solve
$$p - 2q = 3x^2 \sin(y+2x)$$
. (5)

b) Solve $r + s - 6t = y \sin x$. (6)

OR

20 a) Solve
$$x(y-z)p + y(z-x)q = z(x-y)$$
. (5)

b) Solve $(D^2 - 2DD' - 15D'^2) z = 12xy$. (6)

Module V

A tightly stretched string of length L is fixed at both ends. Find the displacement u(x,t) if the string is given an initial displacement f(x) and an initial velocity g(x).

OR

A tightly stretched string with fixed end points x = 0 and x = l is initially in a position given by $u = v_0 sin^3 \left(\frac{\pi x}{l}\right)$, $0 \le x \le l$. If it is released from rest from this position, find the displacement function u(x, t)

A S2035 Pages: 3

Module VI

The ends A and B of a rod of length L are maintained at temperatures 0°C and 100°C respectively until steady state conditions prevails. Suddenly the temperature at the end A is increased to 20°C and the end B is decreased to 60°C.

Find the temperature distribution in the rod at time t.

OR

Find the temperature distribution in a rod of length 2 m whose end points are maintained at temperature zero and the initial temperature is $f(x) = 100(2x-x^2), 0 \le x \le 2$ (10)

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Page 3 of 3

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