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## APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

SECOND SEMESTER M.TECH DEGREE EXAMINATION, MAY 2016

### Electrical & Electronics Engineering

(Control Systems, Guidance and Navigational Control, Electrical Machines, Power System and Control)

#### 01EE6116: SLIDING MODE CONTROL

Time: 3 Hours Max Marks: 60

# Answer any two FULL questions from each part Part A (Modules I & II)

- a. Consider a system described by x = f(x,t,u) with scalar control u subject to discontinuities on some sliding surface given by s(x)=0. Assume that the switch performing the control has a hysteresis. Prove that the velocity vector that will be obtained in the above case is one and the same as that obtained using Filippov's continuation method.
  - b. For an  $n^{th}$  order continuous time system derive a sliding mode control using a reaching law approach based on proportional rate reaching law if the sliding surface is chosen as  $\sigma = c^T x$ .
- 2) a. Design a sliding surface using eigen value placement for the system described by

$$\dot{x} = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 3 \\ 1 & 0 & 1 \end{bmatrix} x + \begin{bmatrix} 0 & 1 \\ 1 & -1 \\ -1 & 0 \end{bmatrix} u$$
(6)

b. Differentiate between sliding mode control and variable structure control with the help of an example. (3)

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b. Derive an expression for a non switching based sliding mode control of a discrete time SISO system subjected to parametric variations in system matrix and is also subjected to external disturbances.

## Part C (Modules V& VI)

- 7) a. Briefly explain the design of an Utkin observer for an LTI system. (6)
  - b. Explain the term relative degree and order w.r.t to sliding mode control system. (4)
  - c. For a system described by

$$\dot{x}_1 = x_2, \dot{x}_2 = x_3, \dot{x}_3 = x_4, \dot{x}_4 = u$$

and assume a sliding surface  $\sigma = c_1x_1 + c_2x_2 + x_3$  is designed. Find the reative degree w.r.t  $\sigma$  for the above system. Is it possible to design a classical SMC for the above system with the above sliding surface if not why?. (2)

- a. Prove that in an Utkin's sliding mode observer sliding mode will takes place in finite time.
  - Explain in detail design of a second order sliding mode controller that will provide a continuous control.
- a. Explain the need of an observer. Also, compare the features of a sliding mode observer and Leunberger observer. Also mention their respective observer dynamics and error dynamics.
  - b. Explain in detail design of a super-twisting based differentiator. (6)

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b. Derive an expression for a non switching based sliding mode control of a discrete time SISO system subjected to parametric variations in system matrix and is also (4) subjected to external disturbances.

## Part C (Modules V& VI)

- a. Briefly explain the design of an Utkin observer for an LTI system. (6)
  - b. Explain the term relative degree and order w.r.t to sliding mode control system. (4)
  - c. For a system described by

$$\dot{x}_1 = x_2, \dot{x}_2 = x_3, \dot{x}_3 = x_4, \dot{x}_4 = u$$

and assume a sliding surface  $\sigma = c_1x_1 + c_2x_2 + x_3$  is designed. Find the reative degree w.r.t σ for the above system. Is it possible to design a classical SMC for the above system with the above sliding surface if not why?. (2)

- 8) a. Prove that in an Utkin's sliding mode observer sliding mode will takes place in finite (6) time.
  - b. Explain in detail design of a second order sliding mode controller that will provide a continuous control. (6)
- 9) a. Explain the need of an observer. Also, compare the features of a sliding mode observer and Leunberger observer. Also mention their respective observer dynamics and error dynamics. (6)
  - Explain in detail design of a super-twisting based differentiator. (6)